

EX-1 A hollow shaft of 200mm inside dia and 300mm outside dia is transmitting 2500KW at 200RPM. Calculate shear stress induced in the shaft.

SOLUTION:-

- D= 300 mm
- d = 200 mm
- P = 2500KW
- N = 200RPM
- $\tau = \text{????}$

1. Find Twisting moment

$$\begin{aligned}M_t &= \frac{\text{KW} \times 10^6 \times 60}{2\pi N} \quad (\text{N.mm}) \\ &= 2500 \times 10^6 \times 60 / (2 \times \pi \times 200) \\ &= 119.36 \times 10^6 \text{ N -mm}\end{aligned}$$

2. Find shear stress

$$\begin{aligned}M_t &= \frac{\pi}{16} \left[\frac{D^4 - d^4}{D} \right] \times [\tau] \\ \tau &= 16 \times 300 \times 119.36 \times 10^6 / (\pi \times (300^4 - 200^4)) \\ \tau &= \mathbf{28.06 \text{ N/mm}^2}\end{aligned}$$

EX-2 A hollow shaft of 240mm inside dia and 320mm outside dia is transmitting 2240KW at 120RPM. Calculate shear stress induced in the shaft.

SOLUTION:-

- D= 320 mm
- d = 240 mm
- P = 2240 KW
- N = 120 RPM
- $\tau = \text{????}$

1. Find Twisting moment

$$M_t = \frac{KW \times 10^6 \times 60}{2\pi N} \quad (\text{N.mm})$$
$$= 2240 \times 10^6 \times 60 / (2 \times \pi \times 120)$$
$$= 178.28 \times 10^6 \text{ N*mm}$$

2. Find shear stress

$$M_t = \frac{\pi}{16} \left[\frac{D^4 - d^4}{D} \right] \times [\tau]$$

$$\tau = 16 \times D \times M_t / (\pi \times (D^4 - d^4))$$

$$\tau = 16 \times 320 \times 178.28 \times 10^6 / (\pi \times (320^4 - 240^4))$$

$$\tau = 40.53 \text{ N/mm}^2$$

EX-3. A solid shaft is transmitting 1MW power at 240 RPM. Determine diameter of shaft if maximum torque transmitted exceeds mean torque is 20%. Assume maximum allowable shear stress is 60 Mpa.

SOLUTION:-

- $P = 1 \text{ MW} = 1000 \text{ KW}$
- $N = 240 \text{ RPM}$
- $\tau = 60 \text{ Mpa} = 60 \text{ N/mm}^2$
- $d = ???$

1. Find Torque

$$M_t = \frac{\text{KW} \times 10^6 \times 60}{2\pi N} \quad (\text{N.mm})$$

$$T = 1000 \times 10^6 \times 60 / (2 \times \pi \times 240)$$

$$T = 39.78 \times 10^6 \text{ N-mm}$$

2. Maximum torque

$$T_{\text{max}} = T + (20\% \text{ of } T)$$

$$= T + (0.2 \times T)$$

$$= 1.2 \times T$$

$$= 1.2 \times 39.78 \times 10^6$$

$$T_{\max} = 47.73 \times 10^6 \text{ N-mm}$$

3. Dia of solid shaft

$$M_t = \frac{\pi}{16} d^3 \times [\tau]$$

$$T_{\max} = (\pi / 16) \times d^3 \times \tau$$

$$d^3 = 16 \times T_{\max} / (\pi \times \tau)$$

$$d^3 = 16 \times 47.73 \times 10^6 / (\pi \times 60)$$

$$d = 159.41 \text{ mm}$$

EX-4 A hollow shaft is transmitting 20 KW at 300 RPM. If diameter ratio is 0.8 and allowable shear stress for the shaft material is 55 MPa, find thickness of shaft.

SOLUTION:-

- $P = 20 \text{ KW}$
- $N = 300 \text{ RPM}$
- $d/D = 0.8$, $d = 0.8 * D$
- $\tau = 55 \text{ MPa} = 55 \text{ N/mm}^2$
- $t = \text{????}$

1. Find Torque

$$M_t = \frac{\text{KW} \times 10^6 \times 60}{2\pi N} \quad (\text{N.mm})$$

$$= 20 \times 10^6 \times 60 / (2\pi \times 300)$$

$$= 636.61 \times 10^3 \text{ N-mm}$$

2. Find diameter

$$M_t = \frac{\pi}{16} \left[\frac{D^4 - d^4}{D} \right] \times [\tau]$$

$$= (\pi \times (D^4 - 0.8^4 D^4) \times 55) / (16 \times D) \quad (1 - 0.8^4) = 0.59$$

$$M_t = (\pi \times D^3 \times 0.59 \times 55) / 16$$

$$D^3 = 16 \times M_t / (\pi \times 0.59 \times 55)$$

$$= 16 \times 636.61 \times 10^3 / (\pi \times 0.59 \times 55)$$

$$= 99.91 \times 10^3$$

$$D = 46.40 \text{ mm} = 48 \text{ mm}$$

$$\text{Inside dia } d = 0.8 \times D$$

$$d = 0.8 \times 48$$

$$= 38.40 \text{ mm}$$

$$= 40 \text{ mm}$$

3. Thickness of Shaft

$$t = (D - d) / 2$$

$$= (48 - 40) / 2$$

$$t = 4 \text{ mm}$$

